

# Category Theory

## Exercise Sheet 1

**Exercise 1.** Find several examples of categories and functors from some of the other lectures which you are attending, and show that these satisfy the definition of a category (resp. a functor).

**Exercise 2.** Show that the identity morphisms in a category are uniquely determined. That is, for each object  $c$  of a category  $C$ , show that there exists a unique element  $\text{id}_c \in \text{Hom}(c, c)$  such that for all objects  $d$  of  $C$  and for all  $f \in \text{Hom}(c, d)$  (resp. all  $f \in \text{Hom}(d, c)$ ) we have  $f \circ \text{id}_c = f$  (resp.  $\text{id}_c \circ f = f$ ).